

C2 Geometric Series Questions

Specimen

4. (a) A geometric series has first term a and common ratio r . Prove that the sum of the first n terms is given by

$$S_n = \frac{a(1-r^n)}{1-r}.$$

Given that $|r| < 1$, write down the sum to infinity of the series. [4]

- (b) The sum to infinity of a geometric series is four times the first term of the series. Find the common ratio. [4]

2005 Winter

8. (a) A geometric series has first term a and common ratio r . Prove that the sum of the first n terms is given by

$$S_n = \frac{a(1-r^n)}{1-r}.$$

Given that $|r| < 1$, write down the sum to infinity of the series. [4]

- (b) The sum to infinity of a geometric series is equal to 4. The sum of the first two terms of the series is 3. Find the common ratio, given that it is positive. [5]

2005 Summer

4. The sum of the first two terms of a geometric series is 6.4, and the sum to infinity of the series is 10.

(a) Given that the common ratio is positive, find its value. [5]

(b) Find, correct to three decimal places, the sum of the first eleven terms of the series. [3]

2006 Winter

4. (a) A geometric series has first term a and common ratio r . Write down the n th term of the series and prove that the sum of the first n terms is given by

$$S_n = \frac{a(1-r^n)}{1-r}. \quad [4]$$

- (b) The fourth term of a geometric series is 2 and the seventh term is 54.

- Find the common ratio of the series.
- Find the sum of the first ten terms of the series, giving your answer correct to one decimal place.
- Find the least value of n for the n th term to exceed 125 000. [10]

2006 Summer

5. The second term of a geometric series is nine times the fourth term of the series.

- Find the possible values of the common ratio. [4]
- Given that the common ratio is positive and the sum to infinity of the series is 12, find the third term of the series. [3]

2007 Winter

3. (a) A geometric series has first term a and common ratio r . Write down the n th term and prove that the sum of the first n terms is given by

$$S_n = \frac{a(1-r^n)}{1-r}.$$

Given that $|r| < 1$, write down the sum to infinity of the series. [5]

- (b) The sum of the first term and the second term of a geometric series is equal to twice the sum of the second term and the third term of the series.

- Given that the common ratio of the series is positive, find the value of the common ratio. [4]
- The sum to infinity of the series is 12. Find, correct to two decimal places, the sum of the first eight terms of the series. [4]

2007 Summer

5. (a) A geometric series has first term a and common ratio r . Prove that the sum of the first n terms is given by

$$S_n = \frac{a(1-r^n)}{1-r}$$

Given that $|r| < 1$, write down the sum to infinity of the series. [4]

- (b) The sum to infinity of a geometric series with first term a and common ratio r is 10. The sum to infinity of a second geometric series with first term a and common ratio $2r$ is 15.

(i) Find the value of r . [4]

(ii) Find the sum of the first four terms of the **first** series, giving your answer correct to two decimal places. [3]

2008 Winter

4. A geometric series has first term a and common ratio r . The fifth term of the geometric series is 135 and the eighth term is 5.

(a) Show that $r = \frac{1}{3}$ and find the value a . [5]

(b) Find the sum to infinity of the series. [2]

2008 Summer

5. A geometric series has first term a and common ratio r . The sum of the first two terms of the geometric series is 7.2. The sum to infinity of the series is 20. Given that r is positive, find the values of r and a . [6]

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2009 Winter

5. (a) A geometric series has first term a and common ratio r . Prove that the sum of the first n terms is given by

$$S_n = \frac{a(1-r^n)}{1-r} . \quad [3]$$

- (b) Find the sum of the first eighteen terms of the geometric series

$$10 + 9 + 8 \cdot 1 + \dots$$

Give your answer correct to the nearest whole number. [3]

- (c) The second term of another geometric series is -4 . The sum to infinity of the series is 9.

- (i) Show that r , the common ratio of the series, satisfies the equation

$$9r^2 - 9r - 4 = 0.$$

- (ii) Find the value of r , giving a reason for your answer. [6]

2009 Summer

5. (a) The ninth and tenth terms of a geometric series are 36 and 108 respectively. Find the seventh term of the geometric series. [3]

- (b) Another geometric series has first term a and common ratio r . The second term of this geometric series is 9 and the sum to infinity of the series is 48.

- (i) Show that r satisfies the equation

$$16r^2 - 16r + 3 = 0.$$

- (974-01) (ii) Find the two possible values for r and the corresponding values of a . [6]

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2010 Winter

5. (a) A geometric series has first term a and common ratio r . Prove that the sum of the first n terms is given by

$$S_n = \frac{a(1-r^n)}{1-r}. \quad [3]$$

- (b) The common ratio of a geometric series is positive. The sum of the first four terms of the series is $73\cdot 8$. The sum to infinity of the series is 125. Find the common ratio and the first term of the geometric series. [6]

2010 Summer

6. (a) Find the sum to infinity of the geometric series $40 - 24 + 14\cdot 4 - \dots$ [3]

- (b) Another geometric series has first term a and common ratio r . The fourth term of this geometric series is 8. The sum of the third, fourth and fifth terms of the series is 28.

- (i) Show that r satisfies the equation

$$2r^2 - 5r + 2 = 0.$$

- (ii) Given that $|r| < 1$, find the value of r and the corresponding value of a . [6]

2011 Winter

5. (a) The second term of a geometric series is 6 and the fifth term is 384.

- (i) Find the common ratio of the series.
(ii) Find the sum of the first eight terms of the geometric series. [6]

- (b) The first term of another geometric series is 5 and the common ratio is $1\cdot 1$.

- (i) The n th term of this series is 170, correct to the nearest integer. Find the value of n .
(ii) Dafydd, who has been using his calculator to investigate various properties of this geometric series, claims that the sum to infinity of the series is 940. Explain why this result cannot possibly be correct. [5]

2011 Summer

5. (a) A geometric series has first term a and common ratio r . Prove that the sum of the first n terms is given by

$$S_n = \frac{a(1-r^n)}{1-r}. \quad [3]$$

- (b) The sum to infinity of a geometric series is equal to four times the first term of the series.

- (i) Find the value of the common ratio of the series.
(ii) Given that the sum of the first two terms of the series is 35, find the sum of the first nine terms of the series. Give your answer correct to the nearest whole number.

[6]

2012 Winter

5. (a) A geometric series has first term a and common ratio r . Prove that the sum of the first n terms is given by

$$S_n = \frac{a(1-r^n)}{1-r}. \quad [3]$$

- (b) The sum of the first two terms of a geometric series is 25.2. The sum to infinity of the series is 30. Given that the common ratio is positive, find the common ratio and first term of this geometric series. [6]

2012 Summer

5. A geometric series has first term a and common ratio r . The sum of the first and second terms of the series is 72. The sum of the first and third terms of the series is 120.

- (a) Show that r satisfies the equation

$$3r^2 - 5r - 2 = 0. \quad [4]$$

- (b) Given that $|r| < 1$, find the value of r and the sum to infinity of the series. [5]

2013 Winter

5. (a) The p th term of a geometric series is 16. The $(p + 1)$ th term of this series is 24. Find the $(p + 4)$ th term of the series. [3]
- (b) The sum of the first three terms of another geometric series is $22\cdot 8$. The sum to infinity of the series is $18\cdot 75$. Find the common ratio and the first term of this geometric series. [6]

2013 Summer

5. (a) Find the sum of the first eighteen terms of the geometric series
 $100 + 80 + 64 + \dots$
Give your answer correct to the nearest whole number. [3]
- (b) The second term of a geometric series is -20 . The sum to infinity of the series is 64.
- (i) Show that r , the common ratio of the series, satisfies the equation
 $16r^2 - 16r - 5 = 0$.
- (ii) Find the value of r , giving a reason for your answer. [6]

2014 Winter

5. A geometric series has first term a and common ratio r . The sum of the second and third terms of the series is -216 . The sum of the fifth and sixth terms of the series is 8.
- (a) Prove that $r = -\frac{1}{3}$. [5]
- (b) Find the sum to infinity of the series. [3]

2014 Summer

5. A geometric series has first term a and common ratio r . The sum of the second and third terms of the series is -216 . The sum of the fifth and sixth terms of the series is 8.
- (a) Prove that $r = -\frac{1}{3}$. [5]
- (b) Find the sum to infinity of the series. [3]

2015

5. (a) The eighth and ninth terms of a geometric series are 576 and 2304 respectively. Find the fifth term of the geometric series. [3]
- (b) Another geometric series has first term a and common ratio r . The third term of this geometric series is 24. The sum of the second, third and fourth terms of the series is -56 .
- (i) Show that r satisfies the equation
- $$3r^2 + 10r + 3 = 0.$$
- (ii) Given that $|r| < 1$, find the value of r and the sum to infinity of the series. [8]

2016

5. (a) A geometric series has first term a and common ratio r . Prove that the sum of the first n terms of the series is given by
- $$S_n = \frac{a(1-r^n)}{1-r}.$$
- [3]
- (b) The sum of the first five terms of a geometric series is 275. The sum to infinity of the series is 243. Find the common ratio and the first term of the geometric series. [6]

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2017

5. A rich businessman makes one donation per year to a certain charity. He starts by donating £100 in the first year. In each subsequent year, the value of the donation is 1.2 times the value of the previous year's donation.
- (a) Find the value of the businessman's donation in the 12th year. Give your answer correct to the nearest pound. [2]
- (b) After receiving the n th donation, the charity's treasurer calculates that over the years, the businessman has donated a **total** of £15474, correct to the nearest pound. Find the value of n . [5]



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